

### Test 3

3 december 2025

Maths IB<sub>2</sub>

subjects : *Probability I*

Tot : [ / 15 marks]

Name: \_\_\_\_\_

#### Problem 1

[ / 7 marks]

A bag contains  $n$  marbles, two of which are blue. Hayley plays a game in which she randomly draws marbles out of the bag, one after another, without replacement. The game ends when Hayley draws a blue marble.

(a) Find the probability, in terms of  $n$ , that the game will end on her

(i) first draw;

(ii) second draw.

[4]

(b) Let  $n = 5$ . Find the probability that the game will end on her

(i) third draw;

(ii) fourth draw.

[4]

#### Problem 2

[ / 9 marks]

Box 1 contains 5 red balls and 2 white balls.

Box 2 contains 4 red balls and 3 white balls.

(a) A box is chosen at random and a ball is drawn. Find the probability that the ball is red. [3]

Let  $A$  be the event that “box 1 is chosen” and let  $R$  be the event that “a red ball is drawn”.

(b) Determine whether events  $A$  and  $R$  are independent. [2]

#### Question 3

The following table shows the probability distribution of a discrete random variable where  $a, k \in \mathbb{R}^+$ .

$x$	1	2	3	4
$P(X=x)$	$k$	$k^2$	$a$	$k^3$

Given that  $E(X) = 2.3$ , find the value of  $a$ .