$Maths \ IB_1 \ HL \hspace{0.5cm} \mbox{Subjects : quadratic eq, logarithms, polyg expansion } \dots$

Total: / 20

Name: Anna

Problem 1 [/4 marks]

Let us consider the equation $\frac{1}{2}x^2 + px + (5p - 12) = 0$

- 1) Find the possible values for p such that the equation has only one root.
- 2) Considering the case when p = 7, give the sum of the two roots.

Problem 2 [/4 marks]

Find A and B such that $\frac{30}{6x^2 - 13x + 6} = \frac{A}{2x - 3} - \frac{B}{3x - 2}$

Problem 3 [/4 marks]

Find y such that : $\log_7(3e^{3y-11}) = \frac{10 + \ln(3)}{\ln(7)}$

Problem 4 [/4 marks]

Find the coefficient of the term in x^4 in the expansion of $\left(2\sqrt{x} - \frac{1}{2}\right)^{10}$

Problem 5 [/4 marks]

Prove by induction $\sum_{j=0}^{n} 2^{j} = 2^{n} - 1$