

Problem 1

Solve the following systems of simultaneous equations :

1) by *substitution* $\begin{cases} x + 3y = 294 \\ 25x + y = -50 \end{cases}$ [5 marks]

2) by *combination* $\begin{cases} \frac{x}{2} + 6y = 17 \\ -x - \frac{3y}{2} = \frac{11}{4} \end{cases}$ [5 marks]

3) by *Cramer* $\begin{cases} \sqrt{27}x + \sqrt{2}y = -\sqrt{2} \\ \sqrt{8}x + \sqrt{3}y = \sqrt{12} \end{cases}$ [5 marks]

4) by the method you want $\begin{cases} 3x + 5y + 1 = 0 \\ 5x + 7y + 11 = 0 \end{cases}$ [5 marks]

5) by the method you want $\begin{cases} \pi x - 3y = -8 \\ -2x + y = 2 \end{cases}$ [5 marks]

Problem 2

i) What is a *singular* system ? [2 marks]

ii) Which of the three following systems is *singular* ? [3 marks]

$$\text{A) } \begin{cases} x - \frac{1}{3}y = -8 \\ -3x + 2y = 2 \end{cases} \quad \text{B) } \begin{cases} \frac{\pi}{2}x - 3y = -8 \\ 0x + y = 2 \end{cases} \quad \text{C) } \begin{cases} 3x - 21y = 19 \\ -2x + 14y = -4 \end{cases}$$

ii) Which of the three following *singular* systems has an *infinite number of solutions* ?

[3 marks]

$$\text{A) } \begin{cases} 12x - 8y = 52 \\ 15x - 10y = 26 \end{cases} \quad \text{B) } \begin{cases} 3x - 21y = 26 \\ -2x + 14y = 52 \end{cases} \quad \text{C) } \begin{cases} -3x - 21y = -52 \\ 2x + 14y = 26 \end{cases}$$

Problem 3

Solve the following system of simultaneous equations, giving x and y in terms of k

$$\begin{cases} x - ky = 1 \\ -3x + 2y = -6 \end{cases}$$

[8 marks]

Bonus

i) – Find the value of k (of problem 3) for having the solution $x = 3$.

– Hence what would be the value for y ?

[+2 marks]

ii) – Find the value of k such that the system (as given in problem 3) is *singular*.

– How many solution(s) would have this singular system ?

[+2 marks]